

SKILLSHEET

Percentage calculations

Percentage of a quantity

A percentage is a fraction 'out of 100'. So, to find a percentage of a number or quantity, you write the percentage as a fraction (or decimal) and multiply it by the quantity.

Example 1

Find:

a 8% of 450

b 47% of \$287

c $17\frac{1}{2}\%$ of \$8974

Solution

Fraction method

$$\mathbf{a} \quad 8\% \text{ of } 450 = \frac{8}{100} \times 450 = 36$$

$$\begin{aligned} \mathbf{b} \quad 47\% \text{ of } \$287 &= \frac{47}{100} \times \$287 \\ &= \$134\frac{89}{100} \\ &= \$134.89 \text{ (press the } \mathbf{ab/c} \text{ key)} \end{aligned}$$

$$\begin{aligned} \mathbf{c} \quad 17\frac{1}{2}\% \text{ of } \$8974 &= 17\frac{1}{2} \div 100 \times \$8974 \\ &= \$1570\frac{9}{20} \\ &= \$1570.45 \text{ (press the } \mathbf{ab/c} \text{ key)} \end{aligned}$$

Decimal method

$$8\% \text{ of } 450 = 0.08 \times 450 = 36$$

$$\begin{aligned} 47\% \text{ of } \$287 &= 0.47 \times \$287 \\ &= \$134.89 \end{aligned}$$

$$\begin{aligned} 17\frac{1}{2}\% \text{ of } \$8974 &= 0.175 \times \$8974 \\ &= \$1570.45 \end{aligned}$$

Exercise

1 Find:

a 88% of 400

b 26% of \$142

c 19% of 1250

d 2% of \$7043

e 58% of 289

f 30% of \$980

g $37\frac{1}{2}\%$ of 824

h 7% of \$56

i 93.1% of 2740

j 3.85% of \$4200

k $6\frac{1}{4}\%$ of 256

l 77.75% of \$3500

Expressing quantities as percentages

To express one quantity as a percentage of another quantity, we first write them as a fraction. (The first quantity, usually the smaller one, forms the numerator [top] of the fraction and the other forms the denominator.) Then we multiply the fraction by 100%. If it is not practical to express the quantities as a fraction, then we divide the first quantity by the second quantity instead.

$$\frac{\text{First quantity}}{\text{Second quantity}} \times 100\% \quad \text{or} \quad \text{First quantity} \div \text{Second quantity} \times 100\%$$

Example 2

- a What percentage is 84 of 90?
- b What percentage is 375 mL of 3 L?
- c What percentage of \$135 is \$60.75?
- d A bike was bought for \$120 and resold for \$145. Express the profit as a percentage (correct to one decimal place) of the cost price.

Solution

$$\text{a} \quad \frac{84}{90} \times 100\% = 93\frac{1}{3}\%$$

$$\text{b} \quad 3 \text{ L} = 3000 \text{ mL}$$

$$\frac{375}{3000} \times 100\% = 12\frac{1}{2}\%$$

$$\text{c} \quad \frac{\$60.75}{\$135} \times 100\% = \$60.75 \div \$135 \times 100\% \\ = 45\%$$

$$\text{d} \quad \text{Profit} = \$145 - \$120 \\ = \$25$$

$$\text{Profit percentage} = \frac{\$25}{\$120} \times 100\% \\ = 20\frac{5}{6}\% \\ = 20.8333 \dots\% \\ \approx 20.8\%$$

Exercise

- 2 a Express 18 out of 40 as a percentage.
- b What percentage is \$56.07 of \$126?
- c What percentage is 105 minutes of 3 hours?
- d What percentage of 2420 is 1694?

- e Mark kicked 8 goals out of eleven attempts. Express his success rate as a percentage, correct to one decimal place.
- f For Sharon's bank account with \$542, the bank paid \$23.30 interest. Calculate the interest rate as a percentage, correct to one decimal place.
- g Henry's share price went from \$4.40 to \$3.75. Calculate the decrease as a percentage (correct to one decimal place) of the original price.
- h Julie's wage increased from \$600 to \$666. Express the increase as a percentage.

Percentage increase and decrease

'Increase' means to make bigger by *adding*. To increase a number or quantity by a percentage, we can calculate that percentage of the original quantity and add it on.

'Decrease' means to make smaller by *subtracting*. To decrease a number or quantity by a percentage, we can calculate that percentage of the original quantity and take it away.

Alternatively, we can increase or decrease the *percentage* that represented the original quantity first to represent the new quantity, then find the new quantity from that adjusted percentage.

Example 3

- a Increase 640 by 12%.
- b Increase \$125 by 7%.
- c Decrease 145 by 20%.
- d Decrease \$2400 by 8.5%.

Solution

Two-step method

- a $12\% \times 640 = 76.8$
 $640 + 76.8 = 716.8$
- b $7\% \times \$125 = \8.75
 $\$125 + \$8.75 = \$133.75$
- c $20\% \times 145 = 29$
 $145 - 29 = 116$
- d $8.5\% \times \$2400 = \204
 $\$2400 - \$204 = \$2196$

One-step method

- Think: Increase by 12% = 100% + 12% = 112%*
 $112\% \times 640 = 1.12 \times 640 = 716.8$
- Think: Increase by 7% = 100% + 7% = 107%*
 $107\% \times \$125 = 1.07 \times \$125 = \$133.75$
- Think: Decrease by 20% = 100% - 20% = 80%*
 $80\% \times 145 = 0.8 \times 145 = 116$
- Think: Decrease by 8.5% = 100% - 8.5% = 91.5%*
 $91.5\% \times \$2400 = 0.915 \times \$2400 = \$2196$

Exercise

- 3 a Increase 140 by 8%.
- b Decrease \$244 by 22%.
- c Increase 750 by 13%.
- d Decrease \$69 by 5%.
- e Increase \$330 by 15.2%.
- f Decrease \$86 by $12\frac{1}{2}\%$.

The unitary method: given a percentage, finding the whole or another percentage

The **unitary method** is so called because we need to find 1% first (*unit* means 'one'). If we are given a percentage of a quantity and asked to find the whole quantity, we use the unitary method to find 1% first, then multiply by 100 to find the whole (100%).

Example 4

- 18% of a number is 45. What is the number?
- 85% of Year 10 went on an excursion. If 102 students went on the excursion, how many are in Year 10?
- The price of a watch after 10% of GST was added was \$92.40. What was the original price of the watch?
- At a '12% off' sale, a game system was reduced to \$215.60. What was the discount?

Solution

- a** 18% of the number = 45

$$\therefore 1\% \text{ of the number} = 45 \div 18 = 2.5$$

$$\therefore 100\% \text{ of the number} = 2.5 \times 100 = 250$$

The required number is 250. (Check: 18% of 250 = 45)

- b** 85% of Year 10 = 102

$$\therefore 1\% \text{ of Year 10} = 102 \div 85 = 1.2$$

$$\therefore \text{Number of Year 10 (100\%)} = 1.2 \times 100 = 120$$

$$\text{(Check: 85\% of 120 = 102)}$$

- c** The original price of the watch was increased by 10%.

$$100\% + 10\% = 110\%$$

$$110\% \text{ of original price} = \$92.40$$

$$\therefore 1\% \text{ of original price} = \$92.40 \div 110 = \$0.84$$

$$\therefore \text{Original price (100\%)} = \$0.84 \times 100 = \$84$$

$$\text{(Check: 110\% of \$84 = \$92.40)}$$

- d** The original price of the game system was decreased by 12%.

$$100\% - 12\% = 88\%$$

$$88\% \text{ of original price} = \$215.60$$

$$\therefore 1\% \text{ of original price} = \$215.60 \div 88 = \$2.45$$

Note that this question asks for the *discount* (12%), not the original price (100%).

$$\therefore \text{Discount (12\%)} = \$2.45 \times 12 = \$29.40$$

$$\text{(Check: Original price} = \text{discount price} + \text{discount}$$

$$= \$215.60 + \$29.40$$

$$= \$245$$

$$\text{Discount price} = 88\% \text{ of } \$245$$

$$= \$215.60)$$

Exercise

- 4 a 15% of an amount is 855. What is the amount?
- b Jane pays 28% of her weekly income in tax. If she pays \$161, then what is her weekly income?
- c Trevor earns 6% commission on every car he sells. If he earned \$1767 from the sale of a car, what was the price of the car?
- d Meikle received \$110.70 interest on her savings account. If the interest rate is 4.5%, how much did Meikle have in her account?
- e The value of a computer fell 7% to \$3250.35. Find its previous price.
- f The population of Westvale increased by 4% to 75 322 this year. What was:
- the population of Westvale last year?
 - the increase?

Answers

- 1** a 352 b \$36.92 c 237.5 d \$140.86
e 167.62 f \$294 g 309 h \$3.92
i 2550.94 j \$161.70 k 16 l \$2721.25
- 2** a 45% b 44.5% c $58\frac{1}{3}\%$ d 70%
e 72.7% f 4.3% g 14.8% h 11%
- 3** a 151.2 b \$190.32 c 847.5 d \$65.55 e \$380.16 f \$75.25
- 4** a 5700 b \$575 c \$29 450 d \$2460
e \$3495 f i 72425 ii 2897